

$$P(B|\Omega H) = \alpha P(B) \sum_f P(f) \sum_r P(r|Bf) P(\Omega|r) P(M|r)$$

$$f_H(r) = \begin{bmatrix} 0.7 \\ 0.01 \end{bmatrix} \begin{matrix} R \\ \bar{R} \end{matrix} \quad f_{\Omega}(r) = \begin{bmatrix} 0.9 \\ 0.05 \end{bmatrix} \begin{matrix} R \\ \bar{R} \end{matrix} \quad f_F(f) = \begin{bmatrix} 0.002 \\ 0.998 \end{bmatrix} \begin{matrix} F \\ \bar{F} \end{matrix}$$

$$f_R(r|Bf) = \begin{bmatrix} 0.95 \\ 0.94 \\ 0.05 \\ 0.06 \end{bmatrix} \begin{matrix} R F \\ R \bar{F} \\ \bar{R} F \\ \bar{R} \bar{F} \end{matrix}$$

$$P(B|\Omega H) = \alpha P(B) \sum_f P(f) \sum_r f_R(r|Bf) \times f_{\Omega}(r) \times f_H(r)$$

$$= \alpha P(B) \sum_f P(f) \sum_r \begin{bmatrix} 0.95 \\ 0.94 \\ 0.05 \\ 0.06 \end{bmatrix} \times \begin{bmatrix} 0.9 \\ 0.05 \end{bmatrix} \times \begin{bmatrix} 0.7 \\ 0.01 \end{bmatrix}$$

$$= \alpha P(B) \sum_f P(f) \sum_r \begin{bmatrix} 0.95 \times 0.9 \times 0.7 \\ 0.94 \times 0.9 \times 0.7 \\ 0.05 \times 0.05 \times 0.01 \\ 0.06 \times 0.05 \times 0.01 \end{bmatrix} \begin{matrix} R F \\ R \bar{F} \\ \bar{R} F \\ \bar{R} \bar{F} \end{matrix}$$

$$\begin{bmatrix} 0.95 \times 0.9 \times 0.7 + 0.05 \times 0.05 \times 0.01 \\ 0.94 \times 0.9 \times 0.7 + 0.06 \times 0.05 \times 0.01 \end{bmatrix} \begin{matrix} F \\ \bar{F} \end{matrix} (*)$$

$$= \alpha P(B) \sum_f f_F(f) f_{\bar{\Omega} H}(Bf) \begin{matrix} (a) \\ (b) \end{matrix}$$

$$\begin{bmatrix} 0.002 \\ 0.998 \end{bmatrix} \times \begin{bmatrix} * \\ * \end{bmatrix}$$

$$= \alpha P(B) [0.002 \times (a) + 0.998 \times (b)] = \alpha P_1$$

$$P(\bar{B}|\Omega H) = \alpha \dots = \alpha P_2$$

$$P(B|\Omega H) + P(\bar{B}|\Omega H) = \alpha (P_1 + P_2) = 1$$

$$\alpha = \frac{1}{P_1 + P_2}$$

$$P(B|\Omega H) = \frac{P_1}{P_1 + P_2}$$