

ℓ^2

L^2

OPTIMIZING ℓ^2

SHAPING PROPERTIES OF PREDICTION ERROR

- REMOVE SLOW DRIFTS

- HIGH-FREQ DISTURBANCES

- ENHANCE/SUPPRESS BY FREQ. WEIGHTING

8 2

$$\mathcal{E}_F(t, \theta) = L(\gamma) \mathcal{E}(t, \theta) = \left[\bar{L}^{-1}(\gamma) H(\gamma, \theta) \right]^{-1} \left[y(t) - G(\gamma, \theta) u(t) \right]$$

SHAPING THE NOISE

$$\ell = \frac{1}{2} \mathcal{E}^2$$

COMPUTATION

ANALYSIS

- STANDARD

→ ROBUST AGAINST BAD DATA → OTHER

- EXPLICIT WEIGHTING:

$$V_N(\theta, z^N) = \frac{1}{N} \sum_{t=1}^N \beta(N, t) \ell(\mathcal{E}_F(t, \theta))$$

3. FREQUENCY-DOMAIN INTERPRETATION OF $\ell = \frac{1}{2} \mathcal{E}^2$ CRITERION FOR LTI SYSTEMS

$$V_N(\theta, z^N) = \frac{1}{N} \sum_{t=1}^N \frac{1}{2} \mathcal{E}^2(t, \theta)$$

$$\mathcal{E}(t, \theta) = \bar{H}^{-1}(\gamma, \theta) [y(t) - G(\gamma, \theta) u(t)]$$

PARSERVAL EQUALITY

$$\|FS\|^2 = \|S\|^2$$

$$V_N(\theta, z^N) = \frac{1}{N} \frac{1}{2} \sum_{n=0}^{N-1} |E_N(2\pi n/N, \theta)|^2$$

IF F ORTHOGONAL
(FOURIER IS)

WITH OVERLOOKING $O(\frac{1}{\sqrt{N}})$ TRANSIENT TERMS

$$E_N(\omega) = \bar{H}^{-1}(e^{j\omega}, \theta) [Y_N(\omega) - G(e^{j\omega}, \theta) U_N(\omega)]$$

$$\begin{aligned} V_N(\theta, z^N) &= \frac{1}{N} \sum \frac{1}{2} |\bar{H}^{-1}(e^{j\frac{2\pi k}{N}}, \theta)|^2 |Y_N(k) - G(e^{j\frac{2\pi k}{N}}, \theta) U_N(k)|^2 \\ &= \frac{1}{N} \frac{1}{2} \sum \underbrace{|\hat{G}_N(e^{j\frac{2\pi k}{N}}) - G(e^{j\frac{2\pi k}{N}}, \theta)|^2}_{Q(k, \theta)} \frac{|U_N(k)|^2}{|H(e^{j\frac{2\pi k}{N}}, \theta)|^2} \end{aligned}$$

LINE WEIGHTED LS
ESTIMATE OF ETFE

$Q(k, \theta)$

FREQUENCY
WEIGHTING