

KALMAN-SZŰRŐ - lehetőleg legegyszerűbb felrakat

$$X_{t+1} = X_t + w_t \rightarrow X_{t+1} = X_t$$

$$Z_{t+1} = X_t + v_t \sim N(0, \sigma_z)$$

$$F=1, H=1$$

$$\hat{X}_{t+1} = \hat{X}_t + K_{t+1} (Z_{t+1} - \hat{X}_t)$$

$$\sigma_{t+1}^2 = (1 - K_{t+1}) \sigma_t^2$$

$$K_{t+1} = \sigma_t^2 (\sigma_t^2 + \sigma_z^2)^{-1} = \frac{1}{1 + \left(\frac{\sigma_z}{\sigma_t}\right)^2} \rightarrow \phi$$

↑ ∞

$$\hat{X}_{t+1} = \hat{X}_t + \frac{1}{1 + \left(\frac{\sigma_z}{\sigma_t}\right)^2} (Z_{t+1} - \hat{X}_t)$$

$$\sigma_{t+1}^2 = \underbrace{\frac{\left(\frac{\sigma_z}{\sigma_t}\right)^2}{1 + \left(\frac{\sigma_z}{\sigma_t}\right)^2}}_{\gamma < 1} \sigma_t^2$$

ZÖSLA'S - a példához

$$P(X_{t+1} | E_{1:t}) = \sum_{x_t} P(X_{t+1} | x_t) P(x_t | E_{1:t})$$

$$\begin{aligned} \sum & \langle 0.883; 0.117 \rangle \langle 0.7; 0.3 \rangle = \langle 0.6532; 0.3468 \rangle \\ & \langle 0.6532; 0.3468 \rangle \langle 0.7; 0.3 \rangle = \langle 0.5613; 0.4387 \rangle \\ & \langle 0.5613; 0.4387 \rangle \langle 0.7; 0.3 \rangle = \langle 0.5276; 0.4724 \rangle \end{aligned}$$

